

# Socially Acceptable Bipedal Robot Navigation via Social Zonotope Network Model Predictive Control

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# Motivating Social Navigation

Passive  
decision  
making

Proactive  
decision

- **Problem statement:**

- Given the dynamics of the **bipedal robot** and a **goal location** find a motion plan that **promotes social acceptability** for the ego-agent in an **environment containing pedestrians** while **ensuring navigation safety**.

assum

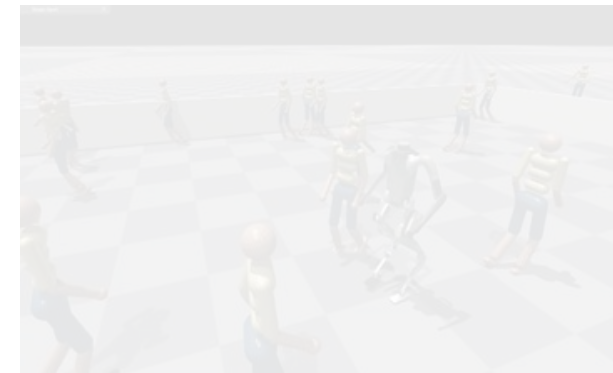
norms

autonomous

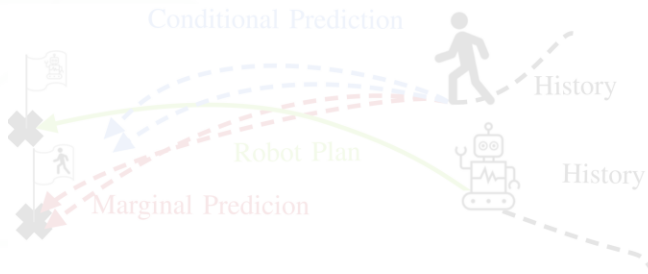
Nominal Online Planning for A Reach-avoid Task



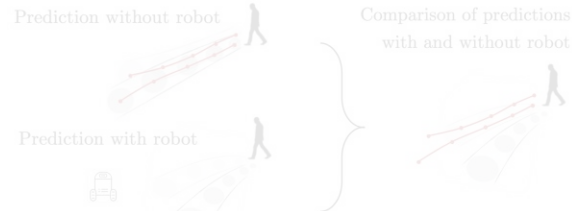
LTL reactive synthesis, belief tracking, formal guarantee on ROM-locomotion and navigation safety



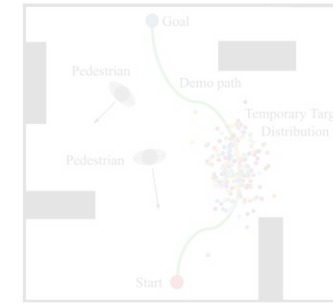
# Social Navigation Literature



[1] Moder, Martin, and Josef Pauli. RO-MAN (2022)



[2] Schaefer, Simon, et al. ICRA (2021)



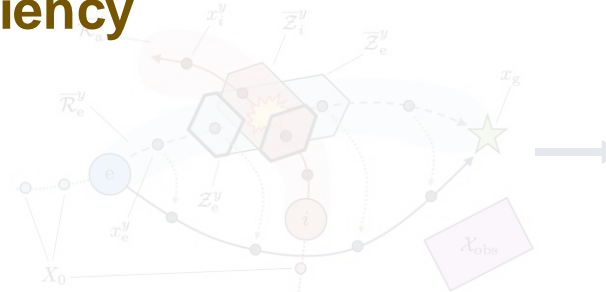
[3] Hong, Yang, et al. TCDS (2023)

Kullback-Leibler divergence as interference metric aim to minimize it

Autoencoder  
stistically

- **Accomplished work:**
  - Learn the socially acceptable path from **real crowd data sets**
  - Learn pedestrians' predictions as **zonotope directly, for computational efficiency**

Assume that minimally-invasive trajectory is the **socially acceptable trajectory**



[4] Papparusso, Luca, et al. ICRA (2024)

**Construct zonotope** over obstacles' Gaussian distribution predictions for ego-agent path planning

# Zonotopes

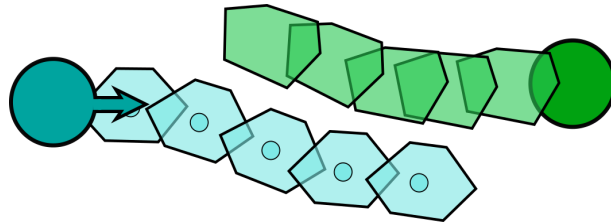
Zonotopes are a convex symmetric polytope

$$\mathbf{Z} = \mathcal{Z}(\mathbf{c}, G) = \{c + \beta_1 g_1 + \beta_2 g_2 + \beta_3 g_3 \mid \beta_i \in [-1, 1]\}$$

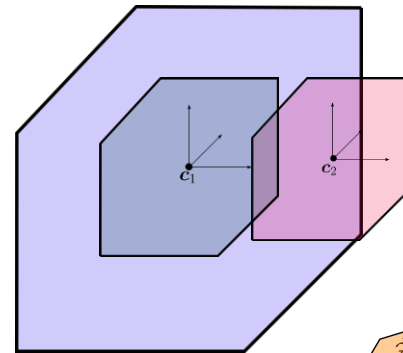
$$G = [g_1, g_2, \dots, g_n] \in \mathbb{R}^{n \times n_G}$$

- Zonotopes offer efficiencies in:

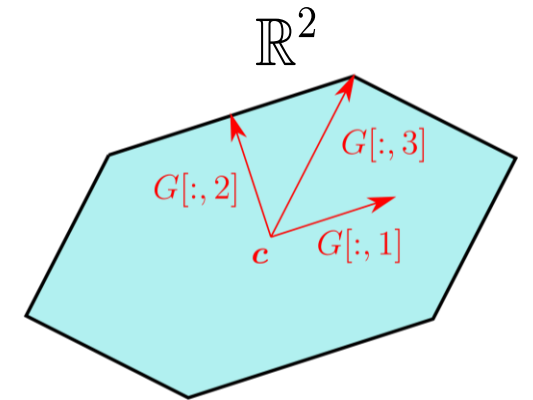
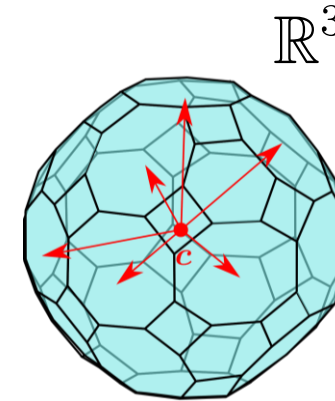
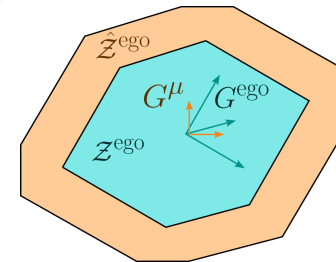
- reachability-based planning



- collision checking [5][6]



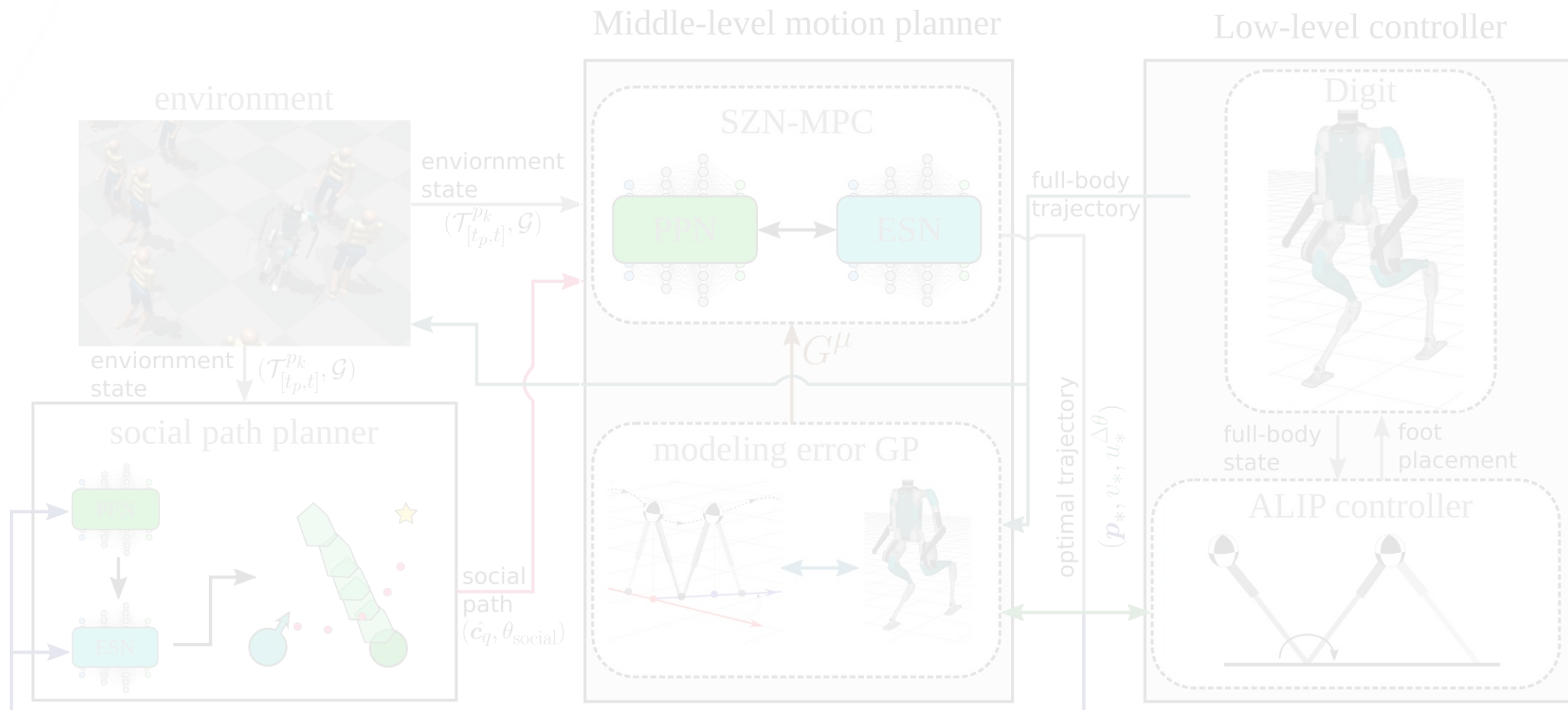
- uncertainty parameterization



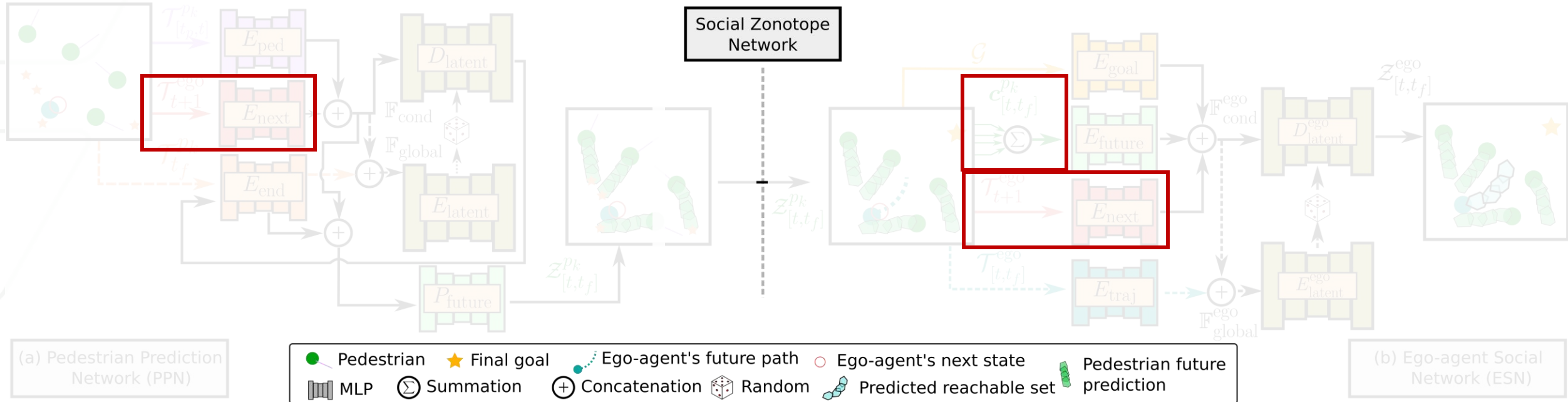
[5] Guibas, Leonidas J, et al. SODA 2003

[6] Althoff, Matthias (2010)

# Bipedal Robot Social Navigation Framework



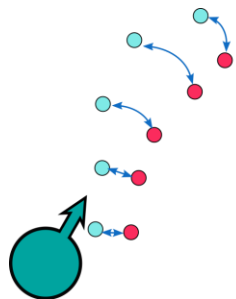
# Social Zonotope Network (SZN)



- **Collective effect** of the surrounding pedestrians, while keeping a fixed architecture
- Conditioning the prediction of the pedestrian's future path on ego-agent's next step
  1. Captures the effect of **the ego-agent's control on pedestrians' future path**
  2. Integrates **SZN-MPC decision's variables** into the neural network

# Zonotope Shaping

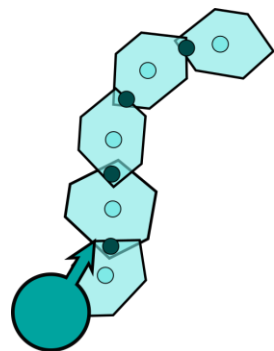
Ground truth tracking



$$\mathcal{L}_{ADE} = \frac{\sum_{i=1}^{t_f-1} \|\mathcal{T}_{\text{mid},i} - \mathbf{c}_i\|}{t_f - 1}$$

$$\mathcal{L}_{FDE} = \|\mathcal{T}_{\text{mid},t_f-1} - \mathbf{c}_{t_f-1}\|$$

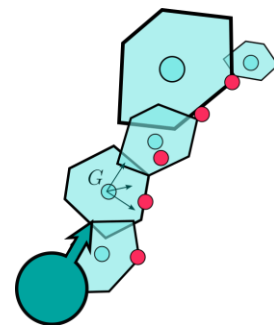
Intersecting zonotopes



$$\mathcal{L}_{\text{prev}} = \sum_{i=0}^{t_f-1} \text{ReLU}(A_i \cdot \mathbf{c}_{\text{mid},i}^p - b_i)$$

$$\mathcal{L}_{\text{next}} = \sum_{i=0}^{t_f-1} \text{ReLU}(A_i \cdot \mathbf{c}_{\text{mid},i}^n - b_i)$$

Size regulation

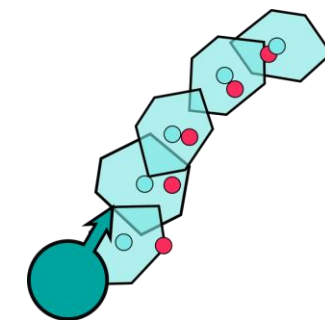









$$\mathcal{L}_G = \|l_G[1] - d_1\| + \|l_G[1:] - d_2\|$$

Digit's physical representation and kinematic limits

Social zonotopes:

$$\mathcal{T}_{[t,t_f]}^{\text{ego}} \in \bigcup_{q=t}^{t_f-1} \mathcal{Z}_q^{\text{ego}}$$



-  Ego agent
-  ego-agent's zonotope
-  Ground truth
-  Displacement error
-  Generators
-  Centers
-  Midpoints between centers

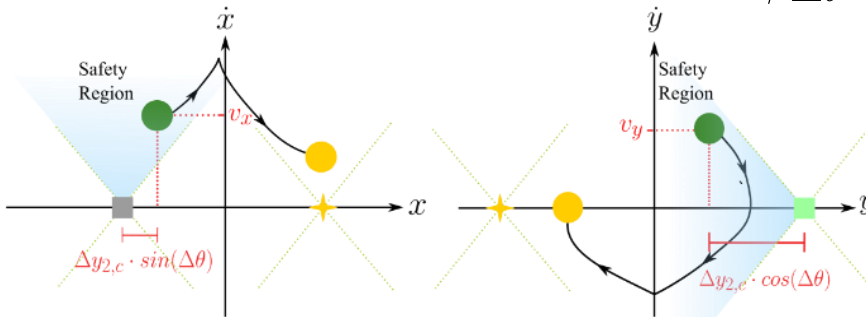
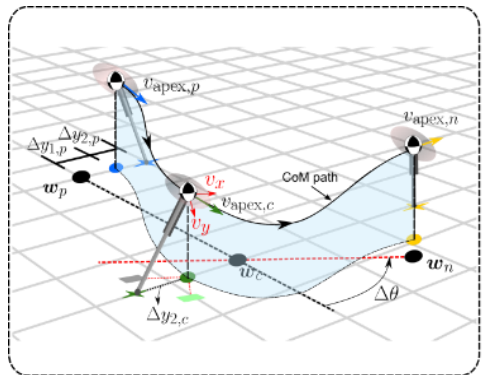
# Locomotion-specific Loss Functions

Real-crowd data sets **do not consider** bipedal robot locomotion **capabilities**

**Locomotion safety loss:** ROM-based loss on step length, velocity and heading change

$\rho(s_t, \phi)$  quantifies **the degree of satisfaction or violation** of the specification  $\phi$  given a specific signal  $s_t$

$$\rho(s_t, \phi) = \begin{cases} \geq 0 & s_t \text{ satisfies } \phi \\ < 0 & s_t \text{ violates } \phi \end{cases}$$



- Locomotion velocity specification:**

$$\phi_{\text{sag}} = \square_{[t+1, t_f]} (s_{[t+1, t_f]}^{v_{\text{sag}}} \leq v_{\text{max}} \wedge s_{[t+1, t_f]}^{v_{\text{sag}}} \geq v_{\text{min}})$$

$$\phi_{\text{lat}} = \square_{[t+1, t_f]} (s_{[t+1, t_f]}^{v_{\text{lat}}} \leq v_{\text{lat}} \wedge s_{[t+1, t_f]}^{v_{\text{lat}}} \geq -v_{\text{lat}})$$

$$\phi_{\text{vel}} = \phi_{\text{sag}} \wedge \phi_{\text{lat}}$$

$$\mathcal{L}_{\phi_{\text{vel}}} = \underbrace{\text{ReLU}(-\rho((s^{v_{\text{sag}}}, s^{v_{\text{lat}}}), \phi_{\text{vel}}))}_{\text{velocity violation}}$$

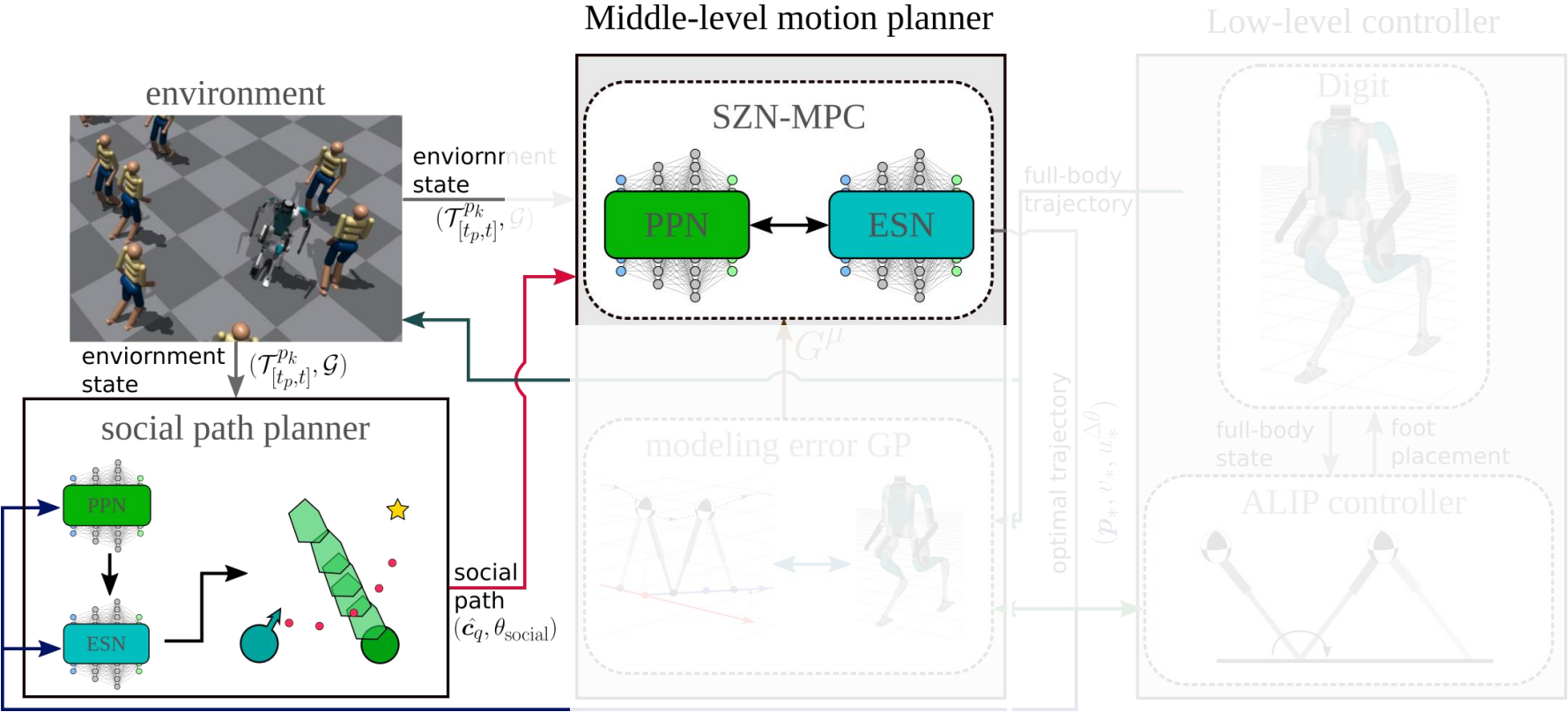
- Heading change specification:**

$$\phi_{\Delta\theta} = \square_{[t+1, t_f]} (s_{[t+1, t_f]}^{\Delta\theta} < \Delta\theta_{\text{max}} \wedge s_{[t+1, t_f]}^{\Delta\theta} > -\Delta\theta_{\text{max}})$$

$$\mathcal{L}_{\phi_{\Delta\theta}} = \underbrace{\text{ReLU}(-\rho(s^{\Delta\theta}, \phi_{\Delta\theta}))}_{\text{heading change violation}}$$



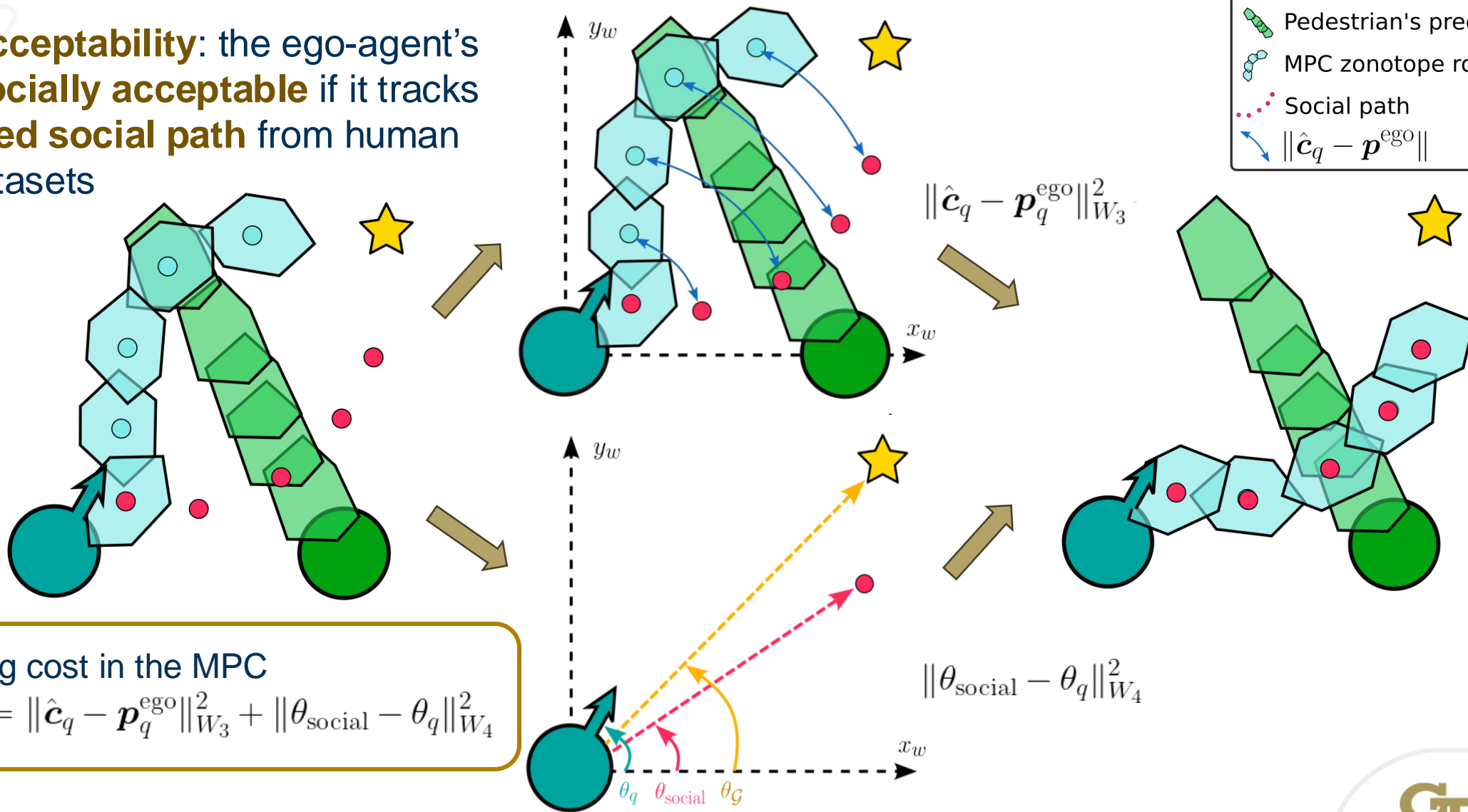
# Social Path Planner



# Social Path Planner

**Social Acceptability:** the ego-agent's path is **socially acceptable** if it tracks the **learned social path** from human crowd datasets

- ★ Final goal
- ♂ Ego agent
- Pedestrian
- ▬ Pedestrian's predicted path
- ⋯ MPC zonotope rollout path
- ⋯ Social path
- ↔  $\|\hat{\mathbf{c}}_q - \mathbf{p}_q^{\text{ego}}\|$



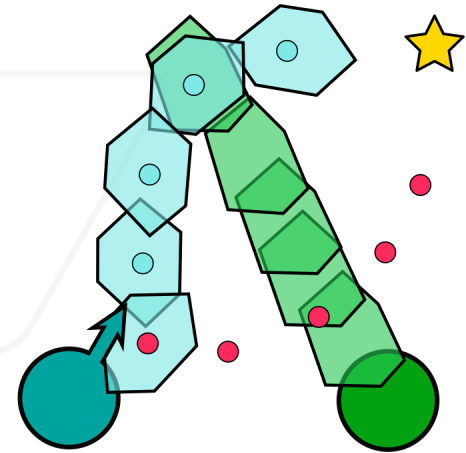
$$\|\hat{\mathbf{c}}_q - \mathbf{p}_q^{\text{ego}}\|_{W_3}^2$$

$$\|\theta_{\text{social}} - \theta_q\|_{W_4}^2$$

• Running cost in the MPC

$$J_{\text{social}}(\mathbf{x}_q) = \|\hat{\mathbf{c}}_q - \mathbf{p}_q^{\text{ego}}\|_{W_3}^2 + \|\theta_{\text{social}} - \theta_q\|_{W_4}^2$$

# SZN-MPC

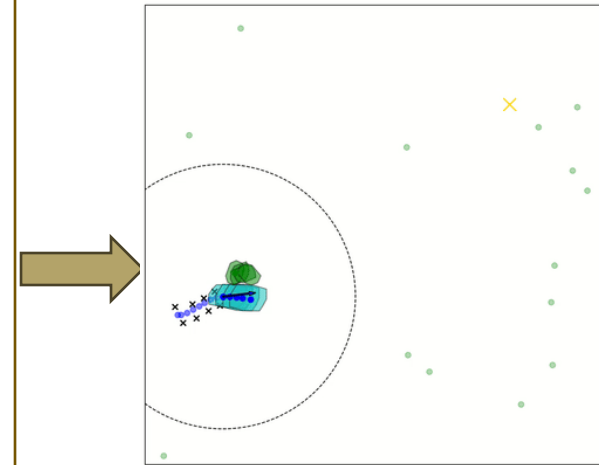


$$\min_{X,U} \sum_{q=0}^{N-1} \Delta \mathbf{u}_q^2 + J(\mathbf{x}, \mathbf{u}) + J_{\text{social}}(\mathbf{x}_q, \mathbf{u}_q)$$

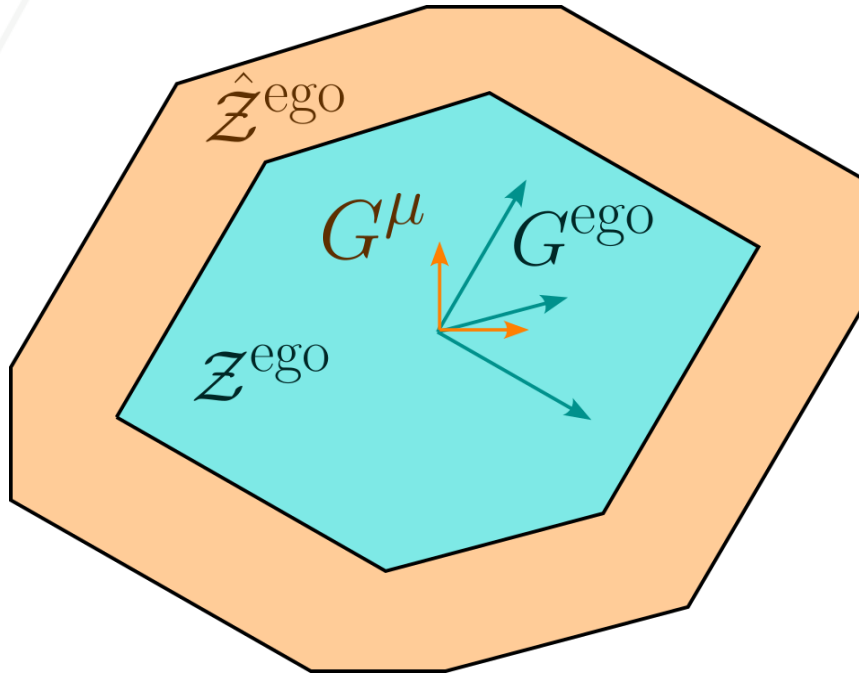
s.t.  $\mathbf{x}_{q+1} = \Phi(\mathbf{x}_q, \mathbf{u}_q)$   
 $\mathbf{x}_0 = \mathbf{x}_{\text{init}}, (\mathbf{x}_q, \mathbf{u}_q) \in \mathcal{XU}_q$   
 $\mathbf{x}_{q+1} \in \mathcal{Z}_{q+1}^{\text{ego}}(\Delta \mathbf{p}_q^{\text{ego}}, E_q)$   
 $\mathcal{Z}_{q+1}^{\text{ego}}(\Delta \mathbf{p}_q^{\text{ego}}, E_q) \cap \mathcal{Z}_{q+1}^{p_{k_q}}(\Delta \mathbf{p}_q^{\text{ego}}) = \emptyset, \forall k_q$

$$\min \sum \text{Control effort} + \text{Distance to goal} + \text{Social path deviation}$$

- s.t. Dynamics constraint  
 Ego-agent's CoM is inside **social zonotope**  
 Ego-agent's **zonotope** does not intersect with **pedestrians' zonotope**

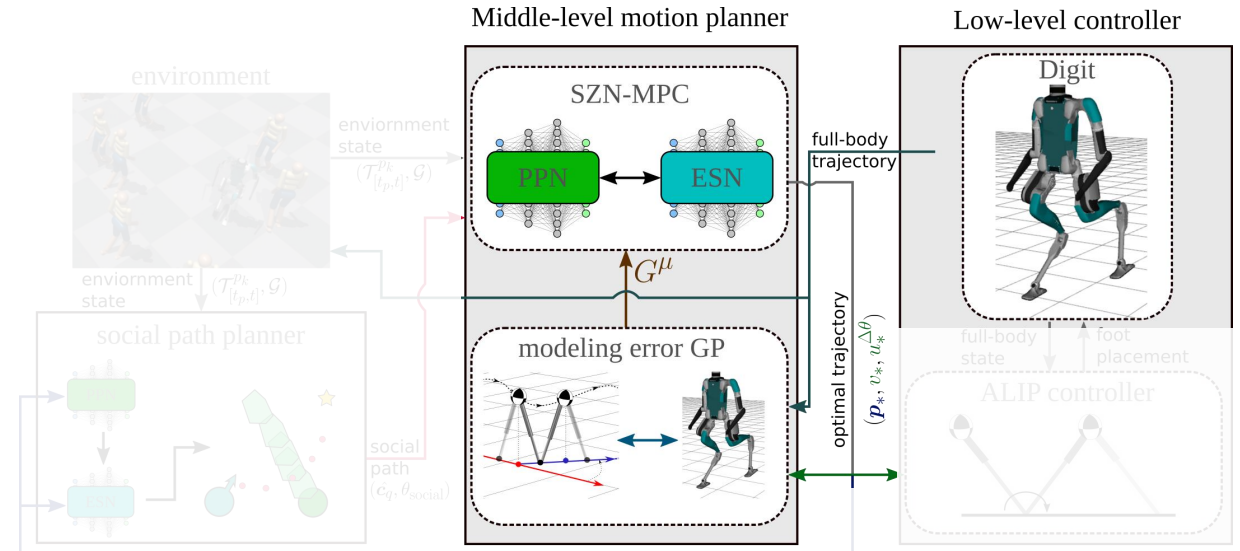


# Uncertainty Quantification



$$G^{\mu} = \begin{pmatrix} \mu_x & 0 \\ 0 & \mu_y \end{pmatrix}$$

$$\hat{z}^{\text{ego}} = \mathcal{L}(c^{\text{ego}}, [G^{\text{ego}} \ G^{\mu}])$$



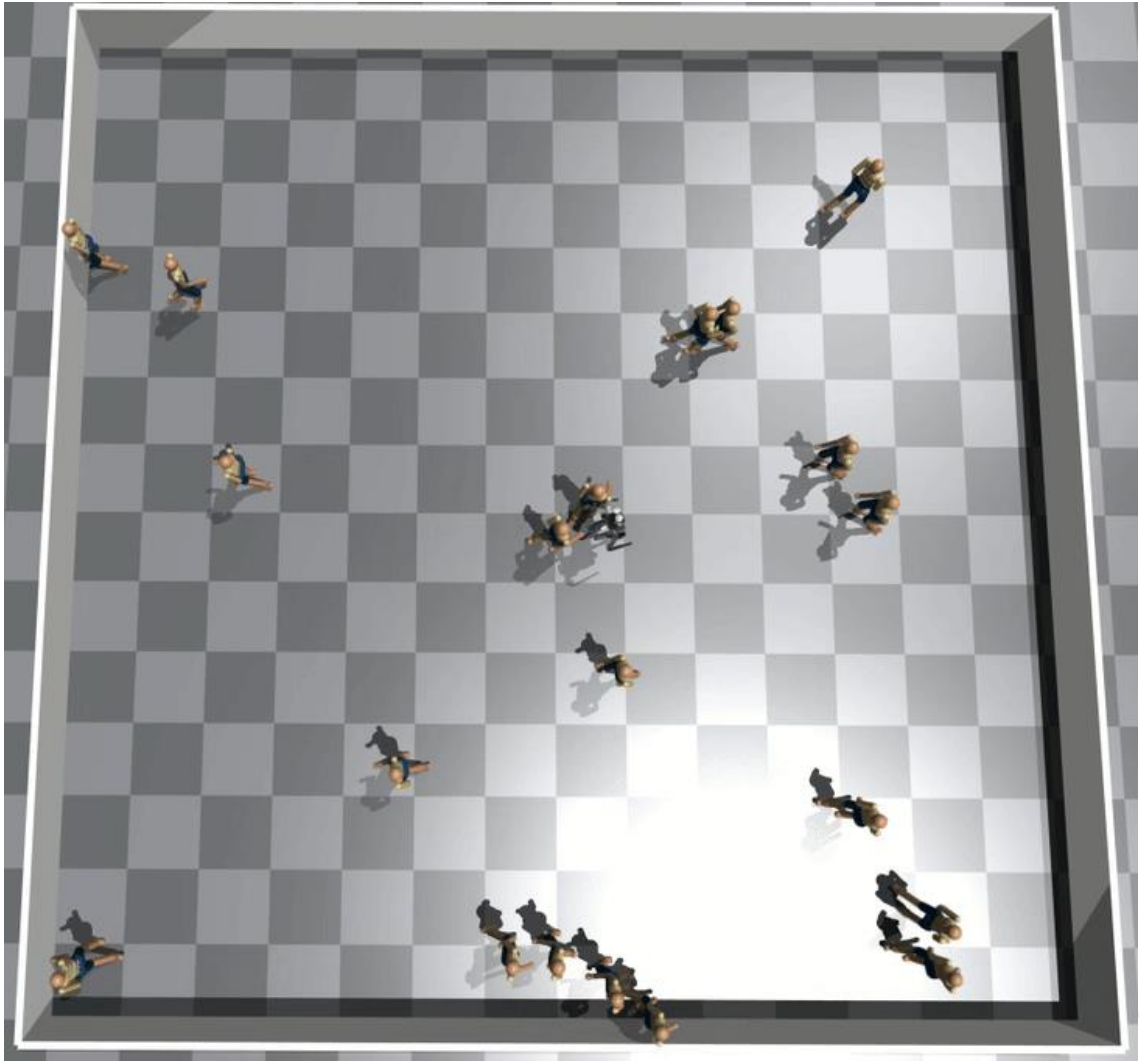
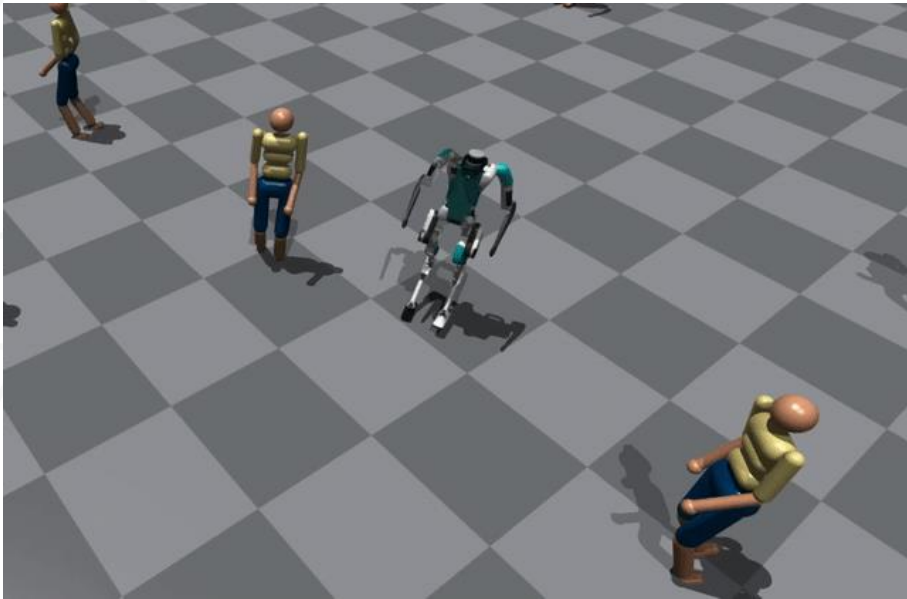
- Introduce a GP that takes as an input:
  - Digit's current velocity
  - SZN-MPC optimal solution
- Outputs the **expected mean deviation**

$$\mu = (\mu_x, \mu_y)$$

**Results: SZN-MPC**

# Simulation Results

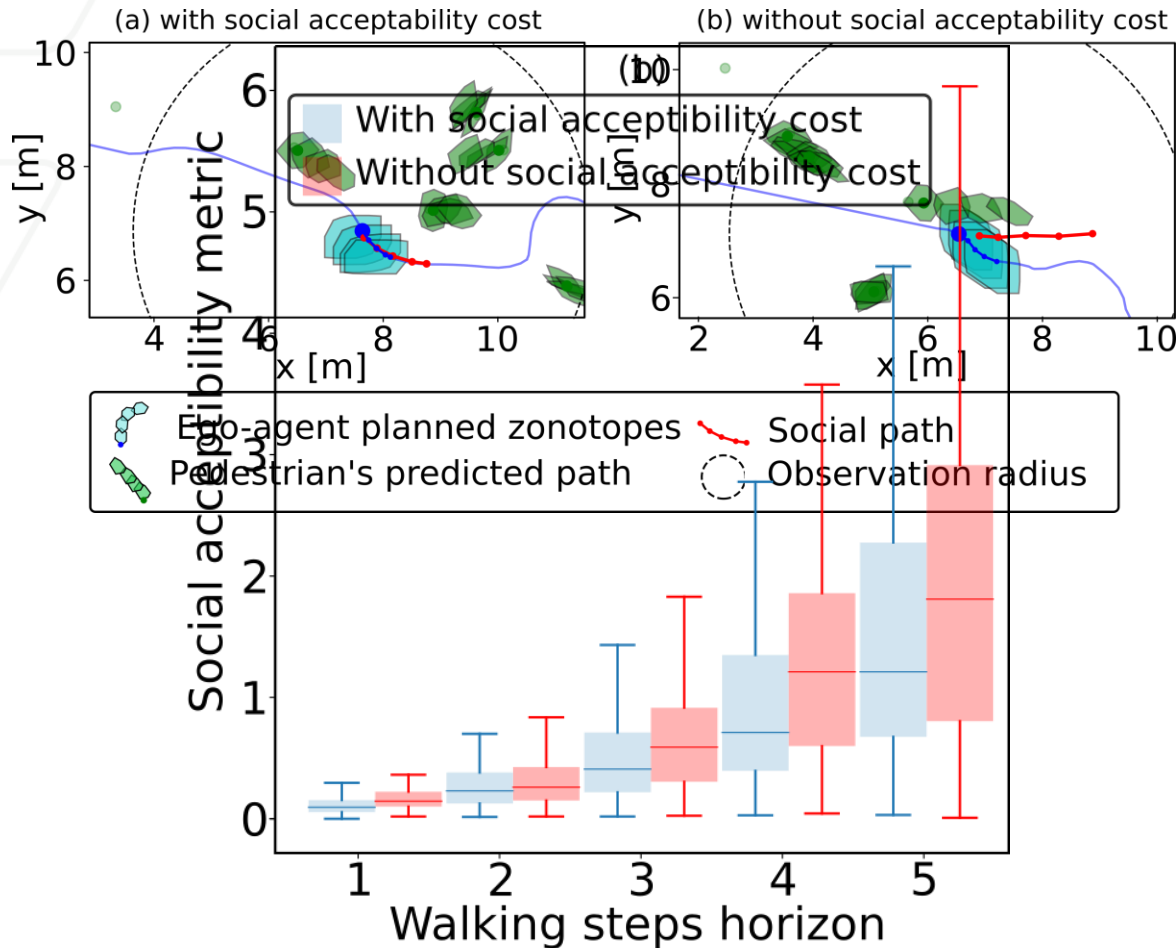
# Results: SZN-MPC



# Results: Social Acceptability Metric and Locomotion Loss

## Social acceptability metric

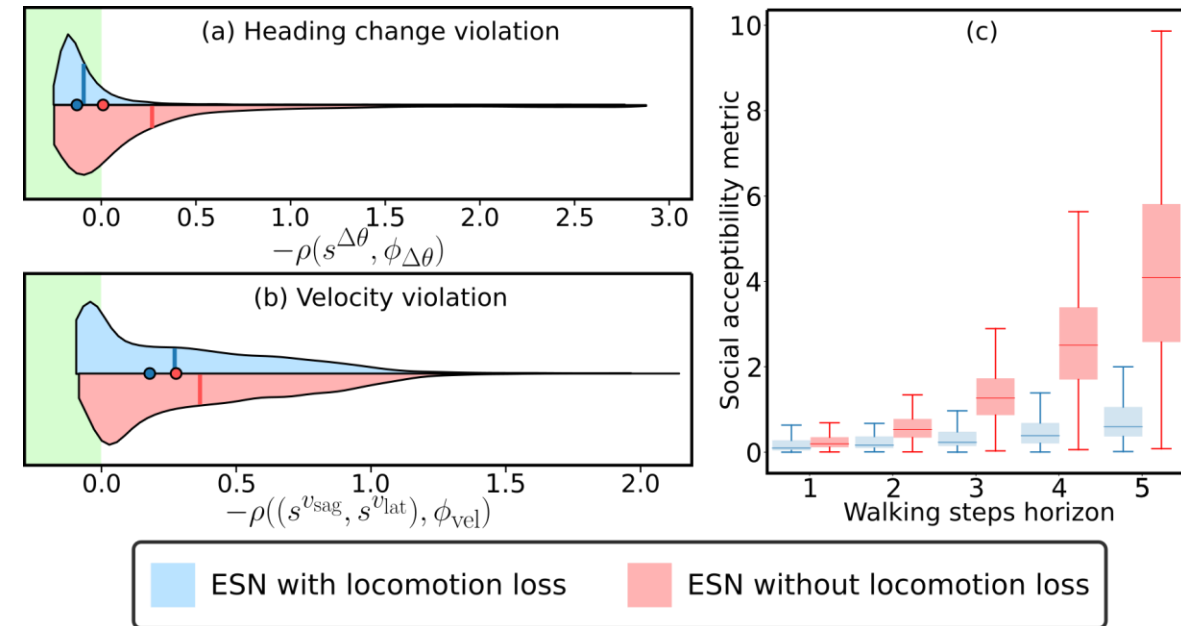
$$J_{\text{social}}(\mathbf{x}_q) = \|\hat{\mathbf{c}}_q - \mathbf{p}_q^{\text{ego}}\|_{W_3}^2 + \|\theta_{\text{social}} - \theta_q\|_{W_4}^2$$



## Locomotion loss

$$\mathcal{L}_{\phi_{\text{vel}}} = \underbrace{\text{ReLU}(-\rho((s^{v_{\text{sag}}}, s^{v_{\text{lat}}}), \phi_{\text{vel}}))}_{\text{velocity violation}}$$

$$\mathcal{L}_{\phi_{\Delta\theta}} = \underbrace{\text{ReLU}(-\rho(s^{\Delta\theta}, \phi_{\Delta\theta}))}_{\text{heading change violation}}$$





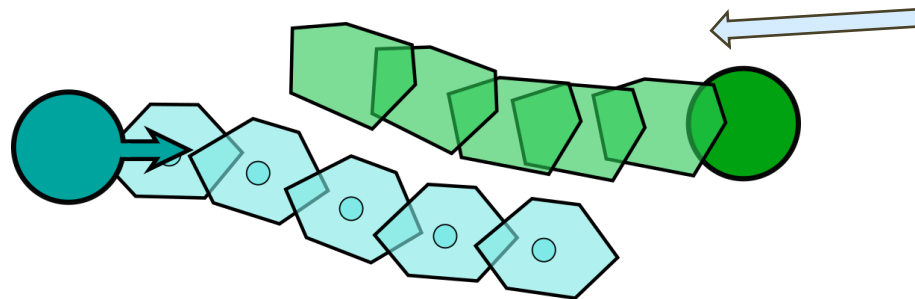
# Results: Benchmarking

- Compare **two versions** of our proposed SZN-MPC with baseline DCBF-MPC [8]

$$h(\mathbf{p}_{q+1}^{\text{ego}}, \mathbf{p}_{k_{q+1}}) \geq (1 - \gamma)h(\mathbf{p}_q^{\text{ego}}, \mathbf{p}_{k_q}) \quad \forall k_q$$

- Coupled SZN-MPC**

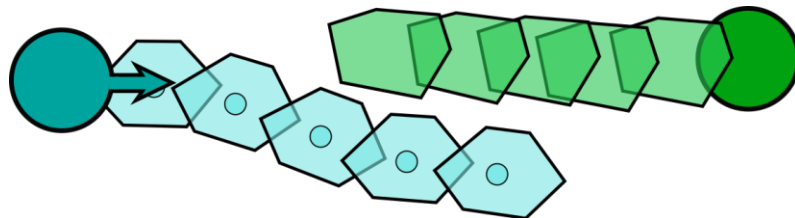
- SZN-MPC optimizes through **both PPN and ESN** networks



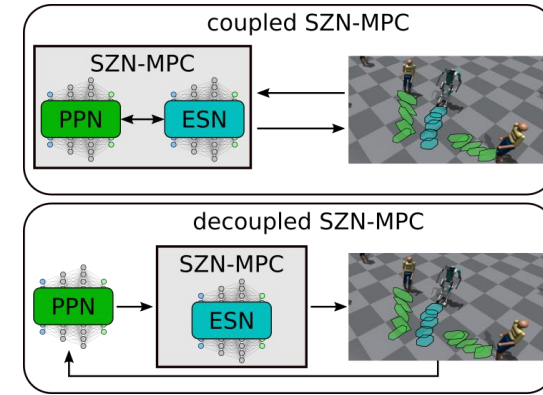
PPN prediction is affected by the ego-agent's future path

- Decoupled SZN-MPC**

- SZN-MPC optimizes through **ESN**, while PPN output **is fixed**



PPN prediction is fixed based on SZN-MPC last optimal solution

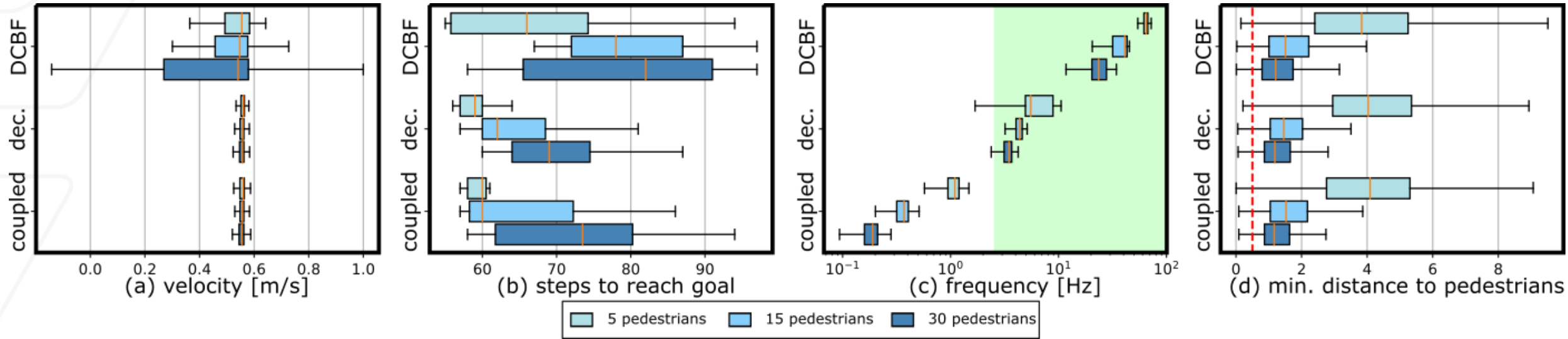


$$\begin{aligned} \min_{X,U} \quad & \sum_{q=0}^{N-1} J(\mathbf{x}, \mathbf{u}) + J_{\text{social}}(\mathbf{x}_q, \mathbf{u}_q) \\ \text{s.t.} \quad & \mathbf{x}_{q+1} = \Phi(\mathbf{x}_q, \mathbf{u}_q) \\ & \mathbf{x}_0 = \mathbf{x}_{\text{init}}, (\mathbf{x}_q, \mathbf{u}_q) \in \mathcal{XU}_q \\ & \mathbf{x}_{q+1} \in \mathcal{Z}_{q+1}^{\text{ego}}(\Delta \mathbf{p}_q^{\text{ego}}, E_q) \\ & \mathcal{Z}_{q+1}^{\text{ego}}(\Delta \mathbf{p}_q^{\text{ego}}, E_q) \cap \mathcal{Z}_{q+1}^{\text{pk}_q}(\Delta \mathbf{p}_q^{\text{ego}}) = \emptyset, \forall k_q \end{aligned}$$

$$\begin{aligned} \min_{X,U} \quad & \sum_{q=0}^{N-1} J(\mathbf{x}, \mathbf{u}) + J_{\text{social}}(\mathbf{x}_q, \mathbf{u}_q) \\ \text{s.t.} \quad & \mathbf{x}_{q+1} = \Phi(\mathbf{x}_q, \mathbf{u}_q) \\ & \mathbf{x}_0 = \mathbf{x}_{\text{init}}, (\mathbf{x}_q, \mathbf{u}_q) \in \mathcal{XU}_q \\ & \mathbf{x}_{q+1} \in \mathcal{Z}_{q+1}^{\text{ego}}(\Delta \mathbf{p}_q^{\text{ego}}, E_q) \\ & \mathcal{Z}_{q+1}^{\text{ego}}(\Delta \mathbf{p}_q^{\text{ego}}, E_q) \cap \mathcal{Z}_{q+1}^{\text{pk}_q} = \emptyset, \forall k_q \end{aligned}$$



# Results: Benchmarking



- **Conservativeness and success rate:** SZN-MPC produce more **consistent velocity, more efficient.**
- **Social Acceptability:** **Predictable behavior** of the ego-agent.
- **Safety and optimality:** SZN-MPC produce **comparable safety** performance, in **fewer steps.**
- **Computational cost:** DCBF is computationally efficient, SZN-MPC can be solved in **real-time** for hardware implementation.

# Standing Group

**Moving randomly**

**Moving randomly**

**Moving in a row**

**Moving in groups**

# Social Navigation Summary

Uncertain environment and obstacles

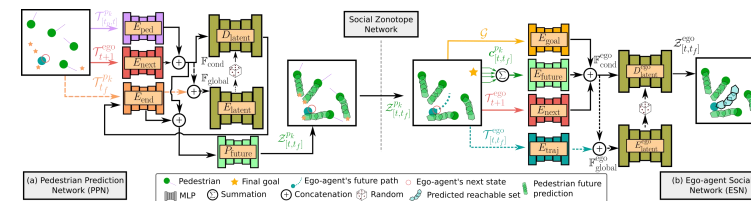
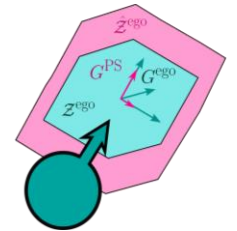
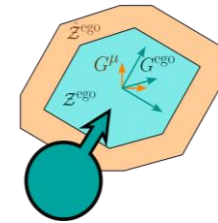
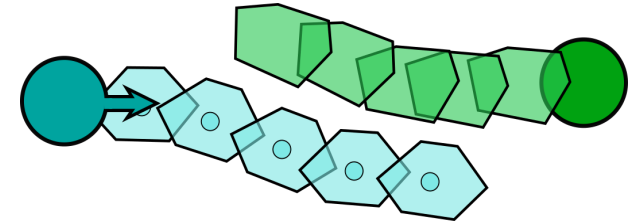
- Human crowds
- Partially observable environment

Uncertain model

- Compensating for learned model errors online
- Reachability-based path planning

Social interaction

- Social path learned from human crowd data sets
- Personal space compensation



# Thank You

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